## Dr. Sophie Marques

## **MAM1020S**

## **Tutorial 3**

August 2017

- 1. (a) Find the range R and the domain D of the real function defined by the rule  $f(x) = \sqrt{4 e^{3x}}$ . Prove that  $f: D \to R$  is one-to-one and onto and compute  $f^{-1}$ . Give the domain and the range for  $f^{-1}$ .
  - (b) Find the range R and the domain D of the real function defined by the rule  $g(x) = \frac{4x-3}{2+3x}$ . Prove that  $g: D \to R$  is one-to-one and onto and compute  $g^{-1}$ . Give the domain and the range for  $g^{-1}$ .
  - (c) Let  $k: A \to B$  and  $l: B \to C$ , prove that if k and l is one-to-one then  $l \circ k$  is one-to-one.
  - (d) Find the range R and the domain D of the real function defined by the rule  $h(x) = \frac{4e^x 3}{2 + 3e^x}$ . Prove that  $h: D \to R$  is one-to-one and onto and compute  $h^{-1}$ . Give the domain and the range for  $h^{-1}$ .
- 2. In this question, we use the function  $y = ce^{kt}$  to model radioactive decay. (You could use a different exponential function, but we want you to get some practice using e.) Plutonium-239 has a half-life of 24400 years. We begin with a sample of 10g.
  - (a) Explain what "half-life" is.
  - (b) Find constants c and k for this situation.
  - (c) How long will it take for the original 10g to decay to 1g?
- 3. (a) Write as a single logarithm

$$\frac{1}{3ln(x)} + \frac{3ln(x+1)}{2ln(x^2+3)}.$$

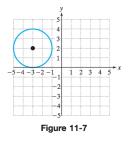
- (b) Solve the inequality:  $ln(\sqrt{x-8}) \le 5$ .
- 4. Identify the center and radius of the circle given by the equation

$$x^2 + y^2 + 2x - 16y + 61 = 0$$

5. Identify the center and radius of the circle given by the equation

$$x^2 + y^2 - 10x + 4y - 7 = 0$$

- 6. Write an equation of the circle shown in Figure 11-7.
- 7. Given: the equation of the parabola



8. Given: the equation of the parabola

$$y = 2x^2 + 4x + 1$$

- (a) Write the equation in standard form.
- (b) Identify the vertex and axis of symmetry. Determine if the parabola opens upward or downward.

- (c) Graph the parabola.
- 9. Given the equation of the parabola  $x = 4y^2$ ,
  - (a) Determine the coordinates of the vertex and the equation of the axis of symmetry.
  - (b) Use the value of a to determine if the parabola opens to the right or left.
  - (c) Plot several points and graph the parabola.
- 10. Given the equation of the parabola  $x = y^2 + 8y 14$ ,
  - (a) Write the equation in standard form.
  - (b) Identify the vertex and axis of symmetry. Determine if the parabola opens upward or downward.
  - (c) Graph the parabola.
- 11. Find the vertex by using the vertex formula.

(a) 
$$x = y^2 + 4y + 5;$$

- (b)  $y = 1/2x^2 3x + 5/2$ .
- 12. Graph the ellipse given by the equation

$$\frac{x^2}{9} + \frac{y^2}{4} = 1$$

13. Graph the ellipse given by the equation

$$25x^2 + y^2 = 25$$

14. Graph the ellipse give by the equation

$$\frac{(x-1)^2}{16} + \frac{(y+3)^2}{4} = 1$$

15. Graph the hyperbola given by the equation

$$\frac{x^2}{36} - \frac{y^2}{9} = 1$$

- (a) Determine whether the transverse axis is horizontal or vertical.
- (b) Draw the reference rectangle and asymptotes.
- (c) Graph the hyperbola and label the vertices.
- 16. Graph the hyperbola given by the equation

$$y^2 - 4x^2 - 16 = 0$$

- (a) Write the equation in standard form to determine whether the transverse axis is horizontal or vertical.
- (b) Draw the reference rectangle and asymptotes.
- (c) Graph the hyperbola and label the vertices.
- 17. Let [[-]] denotes the greatest integer function define in class
  - (a) Compute  $\lim_{t\to 10^{-}} [[-]].$
  - (b) Compute  $\lim_{t\to 10^+} [[-]]$ .
  - (c) Does  $lim_{t\to 10}[[-]]$  exists?

18. Let 
$$F(x) = \frac{x^2 - 4}{|x - 2|}$$

(a) Compute  $\lim_{x\to 2^-} F(x)$ .

- (b) Compute  $\lim_{x\to 2^+} F(x)$ .
- (c) Does  $lim_{x\to 2}F(x)$  exists.
- (d) Sketch a graph for F.
- 19. Compute  $\lim_{t\to 2} \sqrt{t^2 4}\cos(\frac{1}{t-2})$ .
- 20. If  $\lim_{x \to 1} \frac{f(x)-8}{x-1} = 10$  find  $\lim_{x \to 1} f(x)$ .
- 21. The graph of f and g are given. Use then to compute the following limits.

y y	y y
y = f(x)	y = g(x)

(a)  $lim_{t\to 1}4f(t) - 5g(t)$ (b)  $lim_{t\to 2}10f(t) - g(t)$ (c)  $lim_{t\to -1}f(t)g(t)$ 

22.

$$\lim_{t \to 0} \frac{1}{t\sqrt{t+1}} - \frac{1}{t}$$

23.

$$lim_{t\to 9}\frac{3-\sqrt{t}}{9t-t^2}$$